Programming Web Services with Choreography

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FLACOS'09, Toledo, Spain --- September 2009



This Talk In One Slide

- Choreography and Web Services (07)
 - A model for Choreography
 - Session Types
 - Global Calculus
 - About End-Point Projection (EPP)
- Interactional Exceptions and Choreography (08&workinprogress)
 - Session Types and Exceptions
 - Extension of the Global Calculus
 - About End-Point Projection (EPP)



Choreography?

- Choreography as a way of describing communicationbased systems focusing on global message flows
- Idea from WS-CDL, the Web Services Choreography Description Language
- XML-based description language
- **Developed by W3C** (since 2003) in collaboration with private companies Pi4Tech, Adobe, Oracle, Sun, etc.
- π -calculus experts invited since 2004 (R. Milner and us)



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Joint with K. Honda & N. Yoshida



Choreography? (2)

• Choreography as a way of describing communicationbased systems focusing on global message flows

1. Entities have a common goal

- 2. No single point of control
- 3. Only describe communications

"Dancers dance following a global scenario without a single point of control", WS-CDL working group



ALICE

send Bob<"Hello">; receive (z)



ALICE

send Bob<"Hello">;
receive (z)

BOB

receive (x)
send Carl<"Hello">;



ALICE

send Bob<"Hello">;
receive (z)

BOB

receive (x)
send Carl<"Hello">;

CARL

receive (y) send Alice<"Hello">;

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ALICE

send Bob<"Hello">; receive (z)

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CARL

receive (y) send Alice<"Hello">;

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What happens in this system?

Alice writes to Bob, then
Bob writes to Carl, then
Carl writes to Alice

Example: Choreography

Alice \rightarrow Bob <"Hello", x>. Bob \rightarrow Carl <"Hello", y>. Carl \rightarrow Alice <"Hello", z>



Example: comparison

ALICE

send Bob<"Hello">;
receive (z)

BOB

receive (x)
send Carl<"Hello">;

CARL

receive (y)
send Alice<''Hello''>;

Alice \rightarrow Bob <"Hello", x>. Bob \rightarrow Carl <"Hello", y>. Carl \rightarrow Alice <"Hello", z>

- Useful at design stage
- *Abstraction* of a system for formal reasoning
- Monitoring



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Observation & Question

1. Choreography, nice

2. End-point, directly gives implementation of communication primitives



Observation & Question

1. Choreography, nice

2. End-point, directly gives implementation of communication primitives

QUESTION

Can we formally relate 1. and 2.?
Can we define an automated mapping from 1. to 2.?









- Define two models (process algebras):
 - Global Calculus (GC);
 - End-point Calculus (EPC);









Related Work

- **Q. Zongyan et al. [WWW07]** CCS-like approach (similar to ours), no sessions
- Bultan et al.

(Communicating) Finite State Automata

- BIP, REO
- MSC, Protocol Narrations, etc.



Sessions (Types) in two slides...

Channel-based communication:

- two types of channels
 - service channels: ch,... (e.g. services, public channels)
 - session channels: s,t,...(e.g. session id's)
- participants invoke shared channels and
- then they communicate over session channels (s)





• Each service channel ch has a type α:

• ch@B : α

• "ch is located at B and is used as α "

α specifies the direction and the type of each message sent in a session (e.g. over s)

• !(int).?(bool) + !(real).!(real).?(bool)



Service Channel Principle

A service (ch) is always available in many copies



Service Channel Principle

A service (ch) is **always available in many copies**

Alice \rightarrow Bob ch(...). Bob \rightarrow Carl < "Hello", y>.

 $Carl \rightarrow Bob ch (...). ...$

. . .



Global Calculus

(init) I::= $A \rightarrow B : ch(s)$. I $| A \rightarrow B : s < op, e, y > . I$ (com) (cond) if e@A then I₁ else I₂ (sum) | I₁ + I₂ (par) $| I_1 | I_2$ (rec) rec X. I (recVar) X |(vs)I|(res)





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(init) (com) (cond) (sum) (par) (rec) (recVar) (res)



(com) (cond) (sum) (par) (rec) (recVar) (res)

(init)









(init) (com) (cond) (sum) (par) (rec) (recVar) (res)



(init)

(com)

(cond)

(sum)

(par)

(rec)

(res)

(recVar)

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communication happens in the system;
the system becomes I'

$$A \rightarrow B : ch(s). I \qquad \rightarrow (vs) I$$
$$A \rightarrow B : s < op, e, y >. I \qquad \rightarrow I$$





communication happens in the system;
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$$A \rightarrow B : ch(s). I \qquad \rightarrow (vs) I$$
$$A \rightarrow B : s < op, e, y >. I \qquad \rightarrow I[e/y]$$





communication happens in the system;
the system becomes I'

$$(\sigma, A \rightarrow B : ch(s). I) \rightarrow (\sigma, (vs) I)$$
$$(\sigma, A \rightarrow B : s < op, e, y >. I) \rightarrow (\sigma@B[y = \sigma(e)@A], I)$$



An Example

Buyer \rightarrow Seller : ch1(s). Buyer \rightarrow Seller : s(QuoteReq, product, x). Seller \rightarrow Buyer : s(QuoteRes, quote, y). Buyer \rightarrow Seller : s(QuoteAcc, creditcard, z). Seller \rightarrow Shipper : ch2(r). Seller \rightarrow Shipper : r(ShipReq, z, x). Shipper \rightarrow Seller : r(ShipConf). Seller \rightarrow Buyer : s(OrderConf).0


An Example (2)

```
Buyer \rightarrow Seller : ch1(s).
Buyer \rightarrow Seller : s(QuoteReq, product, x).
Seller \rightarrow Buyer : s(QuoteRes, quote, y).
Buyer \rightarrow Seller : s(QuoteAcc, creditcard, z).
Seller \rightarrow Shipper : ch2(r).
...(as before)...
```

÷

Buyer \rightarrow **Seller** : \mathbf{S} (QuoteNoGood) . 0



An Example (3)

Buyer \rightarrow Seller : ch1(s). Buyer \rightarrow Seller : s(QuoteReq, product, x). Seller \rightarrow Buyer : s(QuoteRes, quote, y). if reasonable(y)@Buyer then Buyer \rightarrow Seller : s(QuoteAcc, creditcard, z). Seller \rightarrow Shipper : ch2(r). \cdots (as before) \cdots

else

Buyer \rightarrow **Seller** : \mathbf{S} (QuoteNoGood) . 0



An Example (4)

Buyer \rightarrow Seller : ch1(s). Buyer \rightarrow Seller : s(QuoteReq, product, x). rec X. Seller \rightarrow Buyer : s(QuoteRes, quote, y). if reasonable(y)@Buyer then Buyer \rightarrow Seller : s(QuoteAcc, creditcard, z). Seller \rightarrow Shipper : ch2(r). \cdots (as before) \cdots

else

Buyer \rightarrow **Seller** : \mathbf{s} (QuoteNoGood) . X



End-Point Calculus

P::= *ch(s) . P(serv) | ch!(s). P (req) (in) $| s?(op_1(x_1).P_1 + ... + op_n(x_n).P_n)$ s ! op<e>. P (out) (oplus) $P_1 \oplus P_2$ (par) $|P_1|P_2$ if e then P₁ else P₂ (cond)

(other)

$|\operatorname{rec} X. P | X | (vs) P$



End-Point CalculusP::=*ch (s) . P
ch ! (s) . P
(s? (op_1(x_1).P_1 + ... + op_n(x_n).P_n) (in)
(s ! op>. P
(out)
$$P_1 \oplus P_2$$

(for the product of the product of

(other)

 $| \operatorname{rec} X. P | X | (vs) P$





| rec X. P | X | (vs) P



End-Point Calculus P::= *ch(s) . P(serv) | ch!(s). P (req) (in) $| s?(op_1(x_1).P_1 + ... + op_n(x_n).P_n)$ (out) s ! op<e>. P (oplus) $P_1 \oplus P_2$ (par) $|P_1|P_2$ (cond) if e then P_1 else P_2 | rec X. P | X | (vs) P (other)



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For each session (service) and Seller:

Buyer \rightarrow Seller : ch1(s). Buyer \rightarrow Seller : s(QuoteReq, product, x). Seller \rightarrow Buyer : s(QuoteRes, quote, y). Buyer \rightarrow Seller : s(QuoteAcc, creditcard, z). Seller \rightarrow Shipper : ch2(r). Seller \rightarrow Shipper : r(ShipReq, z, x). Shipper \rightarrow Seller : r(ShipConf). Seller \rightarrow Buyer : s(OrderConf).0



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SELLER

- *ch1(s).
 s ? QuoteReq(x).
- s ! QuoteRes<quote>.
- s ? QuoteAcc(z). ch2!(r).
- **r** ! ShipReq<z>.
- r? ShipConf.
- s! OrderConf



and for Buyer...

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and for Buyer...

Buyer \rightarrow **Seller** : **ch1**(*s*). **Buyer** → **Seller** : S(QuoteRe BUYER Seller

Buyer : S(QuoteRe **Buyer** \rightarrow **Seller** : s (QuoteAc ch1!(s). **Seller** \rightarrow **Shipper** : **ch2**(*r*). **s**!QuoteReq<*product*>. **Seller** \rightarrow **Shipper** : r (ShipRe s?QuoteRes(y). Shipper \rightarrow Seller : r (ShipCc s!QuoteAcc<creditcard>. Seller → Buyer : s(OrderCo s?OrderConf



How does EPP work? (2)

• Careful with participant with multiple services

```
Buyer \rightarrow Seller : ch1(s).
Seller \rightarrow Buyer : s\langle op_1, e_1, x \rangle.
Buyer \rightarrow Seller : ch2(t).
Seller \rightarrow Buyer : t\langle op_2, e_2, y \rangle.
...
Buyer2 \rightarrow Seller : ch2(t).
Seller \rightarrow Buyer2 : t\langle op_3, e_3, y \rangle.
```



How does EPP work? (2)

• Careful with participant with multiple services

```
Buyer \rightarrow Seller : ch1(s).
Seller \rightarrow Buyer : s\langle op_1, e_1, x \rangle.
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Seller \rightarrow Buyer : t\langle op_2, e_2, y \rangle.
...
Buyer2 \rightarrow Seller : ch2(t).
Seller \rightarrow Buyer2 : t\langle op_3, e_3, y \rangle.
```

SELLER *ch1(s). *thread* **s** ! **op**₁<**e**₁>. *ch2!(r). **r** ! op₂<e₂>. thread **r** ! op₃<e₃>.



How does EPP work? (2) • Careful with participant with multiple services **Buyer** \rightarrow **Seller** : **ch1**(**s**). **SELLER Seller** \rightarrow **Buyer** : \mathbf{s} $\langle op_1, e_1, x \rangle$. *ch1(s). **Buyer** \rightarrow **Seller** : **ch2**(*t*). *thread* **s** ! **op**₁<**e**₁>. Seller \rightarrow Buyer : $t \langle op_2, e_2, y \rangle$. NOTE. The EPP guarantees that actions happen in the right order. ₽₂>. 23>. This is not always feasible!!!

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Three principles

Three principles for correct EPP:

- **Connectedness**. A causality principle.
- Well-Threadedness. A local causality principle related to services.
- **Coherence**. Consistent behaviour of the same service over a global description.

This properties can be (in)validated algorithmically



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Connectedness

Good...

- 1. $A \rightarrow B : \mathbf{b}(s)$.
- 2. $A \rightarrow B : s \langle go \rangle$.
- 3. $B \rightarrow C : \mathbf{c}(t) \dots$

Bad...

- a. $A \rightarrow B : \mathbf{b}(s)$. b. $A \rightarrow B : s\langle go \rangle$.
- c. $C \rightarrow D : t \langle \text{hello} \rangle \dots$

b. is "disconnected" from c.

we must synchronise either A or B with either C or D

• connectedness: in $A \rightarrow B \dots C \rightarrow D \dots$ we have B = C.

In general, $\{A, B\} \cap \{C, D\} \neq \emptyset$ – not difficult



Coherence

if x @A then $A \rightarrow B : b(s_1, s_2)$. $A \rightarrow B : s_1 \langle go \rangle$. $B \rightarrow A : s_2 \langle ok \rangle$. $B \rightarrow B : b(s_1, s_2)$. $A \rightarrow B : b(s_1, s_2)$. $A \rightarrow B : s_1 \langle stop \rangle$. $B \rightarrow A : s_2 \langle no \rangle$.

if-branch. $|\mathbf{b}(s_1, s_2) \cdot s_1 \triangleright go \cdot s_2 \triangleleft ok \cdot 0$

else-branch. $|\mathbf{b}(s_1, s_2) \cdot s_1 \triangleright \text{stop} \cdot s_2 \triangleleft \text{no} \cdot \mathbf{0}$

merging the two. $|\mathbf{b}(s_1, s_2) \cdot s_1 \triangleright \begin{bmatrix} go \cdot s_2 \triangleleft ok \cdot \mathbf{0} + \\ stop \cdot s_2 \triangleleft no \cdot \mathbf{0} \end{bmatrix}$

We project each branch onto **B** and merge the results.



Coherence (bad case)

if x@A then $A \rightarrow B : \mathbf{b}(s_1, s_2)$. $A \rightarrow B : s_1 \langle go \rangle$. $B \rightarrow A : s_2 \langle ok \rangle . 0$ else $A \rightarrow B : \mathbf{b}(s_1, s_2)$. $A \rightarrow B : s_1 \langle g o \rangle$. $B \rightarrow A : s_2 \langle no \rangle . 0$



EPP Theorem

The end point projection is:

- Type preserving
- $\mathbf{I} \rightarrow \mathbf{I'}$ implies $\text{EPP}(\mathbf{I}) \rightarrow \text{EPP}(\mathbf{I'})$
- $EPP(I) \rightarrow R$ implies $I \rightarrow I'$ and $EPP(I') \sim R$
- Barb preserving

whenever **I** is well-typed, connected, well-threaded and coherent





- <u>Interactional</u> Exceptions and Choreography (08&workinprogress)
 - Session Types and Exceptions
 - Extension of the Global Calculus
 - About End-Point Projection (EPP)



Exceptions, Literally...

- "An Exception is a person or thing that is excluded from a general statement or does not follow a rule" (Mac Dictionary)
- "Exception (handling) is a programming language construct or computer hardware mechanism designed to handle the occurrence of some condition that changes the normal flow of execution." (Wikipedia)



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Exceptions, in General

try { /* Default Code */ } catch { /* Handler Code */ }

If an exception is thrown by the default code then the handler is executed.

Exceptions are thrown with a special command **throw**



Exceptions and Choreography

What if apply the exception (compensation) idea to *choreography*?

try { /* Default Interaction */ } catch { /* Handler Interaction */ }



Exceptions and Choreography

What if apply the exception (compensation) idea to *choreography*?





A Simple Financial Protocol

1. Buyer \rightarrow Seller : chSeller(s) [s,

2.	$\mathbf{rec} \ X$. Seller $ ightarrow$ Buyer : $s\langle \mathtt{update}, quote, y angle$.
----	--

3. **if** (y < 100)@Buyer then throw else X,

default

handler

 $\texttt{Seller} \to \texttt{Buyer}: s \langle \texttt{conf}, cnum, x \rangle \textbf{.}$

 $\texttt{Buyer} \rightarrow \texttt{Seller} : s \langle \texttt{data}, credit, x \rangle]$



4.

5.

A Financial Protocol with Broker

1. Buyer \rightarrow Broker : **chBroker**(s) [s,



Broker \rightarrow Buyer : s (reject, reason, x)

handler



12.

A Financial Protocol with Broker

- 1. Buyer \rightarrow Broker : chBroker(s) [s,
- 2. Buyer \rightarrow Broker : $s\langle \text{identify}, id, x \rangle$.
- 3. if bad(x)@Broker then throw
- 4. else Broker \rightarrow Seller : chSeller(t)[(s,t), rec X.
- 5. Seller \rightarrow Broker : $t \langle update, quote, y \rangle$.
- 6. Broker \rightarrow Buyer : $s \langle update, 1.1 * y, y \rangle$. default

7. **if** (y < 100)@Buyer then throw else X,

- 8. Seller \rightarrow Broker : $t\langle conf, cnum, x \rangle$.
- 9. Broker \rightarrow Buyer : $s \langle conf, x, x \rangle$.
- 10. Buyer \rightarrow Broker : $s \langle \texttt{data}, credit, x \rangle$.

11. Broker \rightarrow Seller : $t\langle data, x, x \rangle$],

Broker \rightarrow Buyer : $s\langle \text{reject}, reason, x \rangle$]

handler

default



12.

Global Calculus Extension

 $A \rightarrow B : a(s)[\tilde{t}, I, J]$ (init) (inaction) I, J ::=0 $A \rightarrow B : s \langle \mathsf{op}, e, y \rangle . I$ (com) $\mid I \mid J$ (par) throw (throw) | I + J(sum)X if e@A then I else J(recVar) (cond)rec $X \cdot I$ (rec)



End-Points?

P ::=	$!c(\kappa)[P,Q]$	(service)	$\overline{c}(\lambda)[ilde{\kappa},P,Q]$	(request)
	$\mid \kappa ? \Sigma_i op_i \langle x_i \rangle . P_i$	(input)	$\mid \kappa ! op \langle e \rangle$. P	(output)
	P Q	(par)	if e then P else P	(cond)
	0	(inact)	$\mid P\oplus Q$	(choice)
	$\mid X$	(termVar)	$ \mathbf{rec} X \cdot P$	(recursion)
	throw	(throw)		
N ::=	$A[P]_{\sigma} \mid N_1 \mid$	$\mid N_2 \mid \epsilon$		








$\overline{\mathbf{chBroker}}(s^+)[s^+,$

 s^+ !identify $\langle id \rangle$.rec $X . s^+$?update(y).if (y < 100) then throw else X, merge $(s^+$?conf $(x) . s^+$!data $\langle credit \rangle$, s^+ ?reject(x) . P)]





EPP? (Broker)















$*\mathbf{chSeller}(t^{-})[\ \mathbf{rec}\ X \,.\, t^{-}! \mathsf{update}\langle quote \rangle \,.\, X,\ t^{-}! \mathsf{conf}\langle cnum \rangle \,.\, t^{-}? \mathsf{data}(x)\]$



Other Stuff on Choreography

- Choreography as a Session Type (Multiparty Session Types) [@POPL08] [Yoshida et al. @CONCUR08, ESOP09]
- Choreography and Strand Spaces (Security) [PLACES09, ICE09 - jointly with J.Guttman]
- Scribble, a language based on choreography and session types (Pi4Tech, K. Honda, R. Hu)



Work in Progress

- Logic for choreography and Partial Specification
- Annotated Multiparty Session Types
- Secure EPP for Choreography

• Global View Extraction (Inverse of EPP)











Thank you



Well-Threadedness

 $A \rightarrow B : \mathbf{b}(s)$. $A \rightarrow B : s(go).$ $B \rightarrow C : \mathbf{c}(t)$. $C \rightarrow A : \mathbf{a}(r)$. $A \rightarrow C : r \langle hi \rangle$. $C \rightarrow B : t \langle acc \rangle$. $B \rightarrow A : s(ok)$.

 $A \begin{bmatrix} \mathbf{b}(\nu s) \cdot s \triangleleft go \cdot s \triangleright ok \dots \\ ! \mathbf{a}(r) \cdot r \triangleleft hi \dots \end{bmatrix}$

 $\mathbf{B} \begin{bmatrix} \mathbf{1} \mathbf{b}(s) \cdot s \triangleright \mathbf{g} \mathbf{o} \\ \mathbf{\overline{c}}(\nu t) \cdot t \triangleright \mathbf{acc} \cdot s \triangleleft \mathbf{ok} \dots \end{bmatrix}$

C [! $\mathbf{c}(t)$. $\overline{\mathbf{a}}(\nu r)$.r > hi.t < acc...]



Well-Threadedness (2)

Bad... $A \rightarrow B : b(s).$ $A \rightarrow B : s(go).$ $\mathbf{B} \rightarrow \mathbf{C} : \mathbf{C}(t).$ $\mathbf{C} \rightarrow \mathbf{A} : \mathbf{a}(r).$ $\mathbf{A} \rightarrow \mathbf{C} : \mathbf{r} \langle \mathbf{hi} \rangle.$ $\mathbf{C} \rightarrow \mathbf{A} : \mathbf{r} \langle \mathbf{hi} \rangle.$ $A \rightarrow B : s(hello).$

Good... $A \rightarrow B : b(s).$ $A \rightarrow B : s(go).$ $\mathbf{B} \rightarrow \mathbf{C} : \mathbf{C}(t).$ $\mathbf{C} \rightarrow \mathbf{A} : \mathbf{a}(r).$ $A \rightarrow C : r \langle hi \rangle.$ $\mathbf{C} \rightarrow \mathbf{B} : t \langle \mathbf{acc} \rangle.$ $\mathbf{B} \rightarrow \mathbf{A} : s(ok).$



Well-Threadedness (3)

 $A \rightarrow B : b(s).$ $A \rightarrow B : s \langle go \rangle.$ $B \rightarrow C : c(t).$ $C \rightarrow A : a(r).$ $A \rightarrow C : r \langle hi \rangle.$ $C \rightarrow A : r \langle hi \rangle.$ $A \rightarrow B : s \langle hello \rangle.$

 $A \begin{bmatrix} \overline{\mathbf{b}}(s) & s \triangleleft go \\ s \triangleleft hello \\ \mathbf{a}(r) & r \triangleleft hi \\ r \rhd hi \\ \mathbf{P}' \end{bmatrix}$

 $\mathbf{B} \begin{bmatrix} \mathbf{!b}(s), s \triangleright \mathbf{go}, \\ \mathbf{c}(t), \underline{s} \triangleright \mathbf{hello}, Q \end{bmatrix}$

C [!c(t). $\overline{a}(r)$. r > hi. r < hi. S]

















